

Introduction to Parsing Ambiguity and Syntax Errors

Outline

- Regular languages revisited
- Parser overview
- Context-free grammars (CFG's)
- Derivations
- Ambiguity
- Syntax errors

Languages and Automata

- Formal languages are very important in CS
 - Especially in programming languages and compilers
- Regular languages
 - The weakest formal languages widely used
 - Many applications
- We will also study context-free languages

Limitations of Regular Languages

Intuition: A finite automaton that runs long enough must repeat states

- A finite automaton *cannot remember* number of times it has visited a particular state
- because a finite automaton has finite memory
 - Only enough to store in which state it is
 - Cannot count, except up to a finite limit
- Many languages are not regular
- E.g., the language of balanced parentheses is not regular: $\{ ({}^i)^i \mid i \geq 0 \}$

The Functionality of the Parser

- **Input:** sequence of tokens from lexer
- **Output:** parse tree of the program

Example

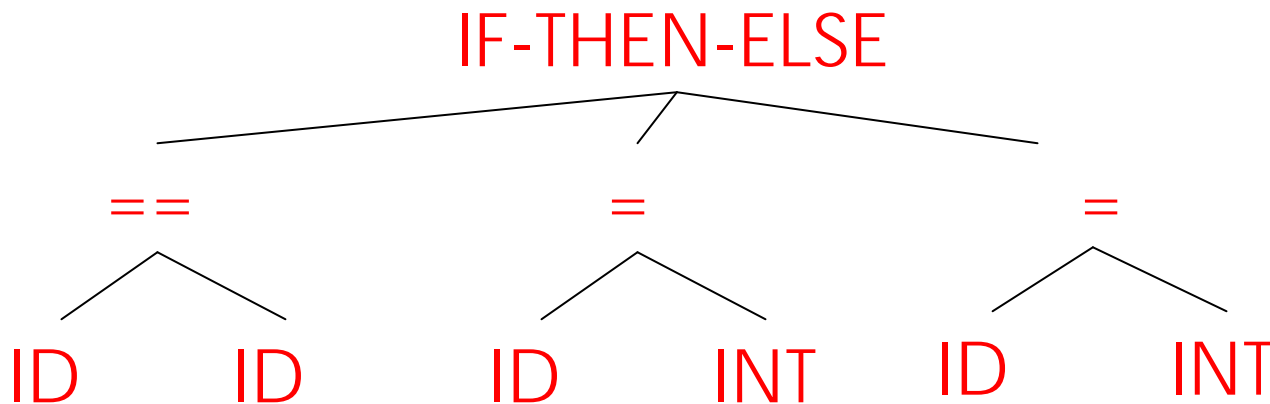
- If-then-else statement

`if (x == y) then z = 1; else z = 2;`

- Parser input

`IF (ID == ID) THEN ID = INT; ELSE ID = INT;`

- Possible parser output



Comparison with Lexical Analysis

<i>Phase</i>	<i>Input</i>	<i>Output</i>
Lexer	Sequence of characters	Sequence of tokens
Parser	Sequence of tokens	Parse tree

The Role of the Parser

- Not all sequences of tokens are programs ...
- Parser must distinguish between valid and invalid sequences of tokens
- We need
 - A language for describing valid sequences of tokens
 - A method for distinguishing valid from invalid sequences of tokens

Context-Free Grammars

- Many programming language constructs have a recursive structure
- E.g. A *STMT* is of the form
 - if *COND* then *STMT* else *STMT* , or
 - while *COND* do *STMT* , or
 - ...
- Context-free grammars are a natural notation for this recursive structure

CFGs (Cont.)

A CFG consists of

- A set of *terminals* T
- A set of *non-terminals* N
- A *start symbol* S (a non-terminal)
- A set of *productions*

Assuming $X \in N$ the productions are of the form

$$X \rightarrow \varepsilon$$

, or

$$X \rightarrow Y_1 Y_2 \dots Y_n$$

where $Y_i \in N \cup T$

Notational Conventions

- In these lecture notes
 - Non-terminals are written upper-case
 - Terminals are written lower-case
 - The start symbol is the left-hand side of the first production

Example: A small fragment of our language:

STMT \rightarrow if COND then STMT else STMT
| while COND do STMT
| id = int

One More Example

Grammar for simple arithmetic expressions:

$$\begin{array}{l} E \rightarrow E * E \\ | E + E \\ | (E) \\ | id \end{array}$$

The Language of a CFG

Read productions as replacement rules:

$$X \rightarrow Y_1 \dots Y_n$$

Means X can be replaced by $Y_1 \dots Y_n$ (in this order)

$$X \rightarrow \varepsilon$$

Means X can be erased (replaced with empty string)

Key Idea

- (1) Begin with a string consisting of the start symbol "S"
- (2) Replace any non-terminal X in the string by the right-hand side of some production

$$X \rightarrow Y_1 \dots Y_n$$

- (3) Repeat (2) until there are no non-terminals in the string

The Language of a CFG (Cont.)

More formally, we write

$$X_1 \cdots X_i \cdots X_n \rightarrow X_1 \cdots X_{i-1} Y_1 \cdots Y_m X_{i+1} \cdots X_n$$

if there is a production

$$X_i \rightarrow Y_1 \cdots Y_m$$

We write

$$X_1 \cdots X_n \xrightarrow{*} Y_1 \cdots Y_m$$

if

$$X_1 \cdots X_n \rightarrow \cdots \rightarrow \cdots \rightarrow Y_1 \cdots Y_m$$

in 0 or more steps

The Language of a CFG

Let G be a context-free grammar with start symbol S . Then the language of G is:

$$\left\{ a_1 \dots a_n \mid S \xrightarrow{*} a_1 \dots a_n \text{ and every } a_i \text{ is a terminal} \right\}$$

Terminals

- Terminals are called so because there are no rules for replacing them
- Once generated, terminals are permanent
- Terminals ought to be tokens of the language

Examples

$L(G)$ is the language of the CFG G

Strings of balanced parentheses $\{(^i)^i \mid i \geq 0\}$

Two equivalent ways of writing the grammar G :

$$\begin{array}{l} S \rightarrow (S) \\ S \rightarrow \varepsilon \end{array} \quad \text{or} \quad \begin{array}{l} S \rightarrow (S) \\ S \rightarrow \varepsilon \end{array}$$

Example

A fragment of our example language (simplified):

STMT \rightarrow if COND then STMT
| if COND then STMT else STMT
| while COND do STMT
| id = int
COND \rightarrow (id == id)
| (id != id)

Example (Cont.)

Some elements of the our language

id = int

if (id == id) then id = int else id = int

while (id != id) do id = int

while (id == id) do while (id != id) do id = int

if (id != id) then if (id == id) then id = int else id = int

Arithmetic Example

Simple arithmetic expressions:

$$E \rightarrow E + E \mid E * E \mid (E) \mid \text{id}$$

Some elements of the language:

id		id + id
(id)		id * id
(id) * id		id * (id)

Notes

The idea of a CFG is a big step.

But:

- Membership in a language is just "yes" or "no"; we also need the parse tree of the input
- Must handle errors gracefully
- Need an implementation of CFG's
 - e.g., [yacc/bison/ML-yacc/...](#)

Derivations and Parse Trees

A *derivation* is a sequence of productions

$$S \rightarrow \dots \rightarrow \dots \rightarrow \dots$$

A derivation can be drawn as a tree

- Start symbol is the tree's root
- For a production $X \rightarrow Y_1 \cdots Y_n$ add children $Y_1 \cdots Y_n$ to node X

Derivation Example

- Grammar

$$E \rightarrow E + E \mid E * E \mid (E) \mid id$$

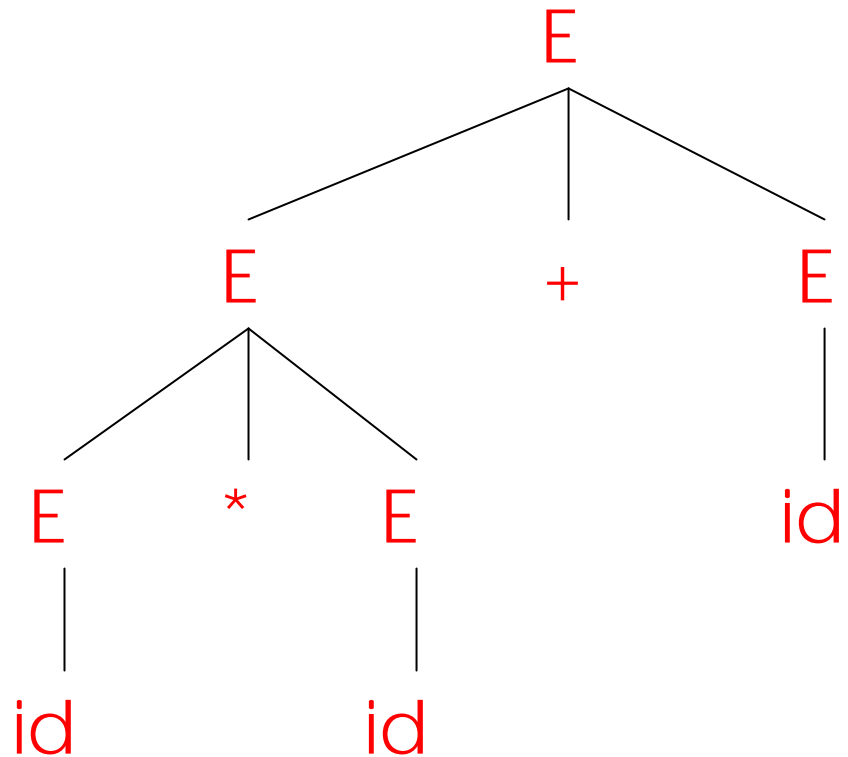
- String

$$id * id + id$$

Derivation Example (Cont.)

$E \rightarrow E+E \mid E * E \mid (E) \mid id$

E
 $\rightarrow E+E$
 $\rightarrow E * E+E$
 $\rightarrow id * E + E$
 $\rightarrow id * id + E$
 $\rightarrow id * id + id$



Derivation in Detail (1)

$E \rightarrow E+E \mid E^*E \mid (E) \mid \text{id}$

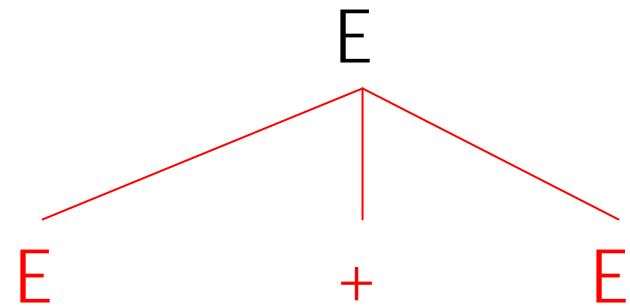
E

E

Derivation in Detail (2)

$E \rightarrow E+E \mid E * E \mid (E) \mid \text{id}$

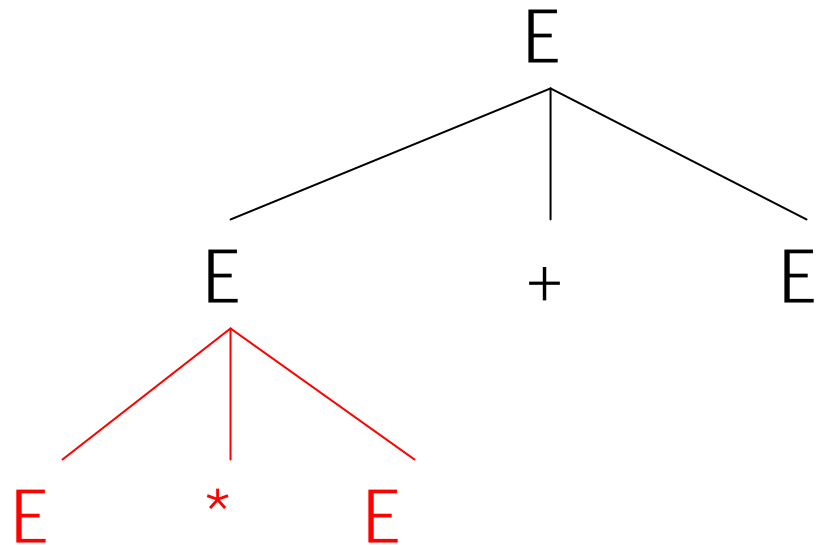
E
 $\rightarrow E+E$



Derivation in Detail (3)

$E \rightarrow E+E \mid E * E \mid (E) \mid \text{id}$

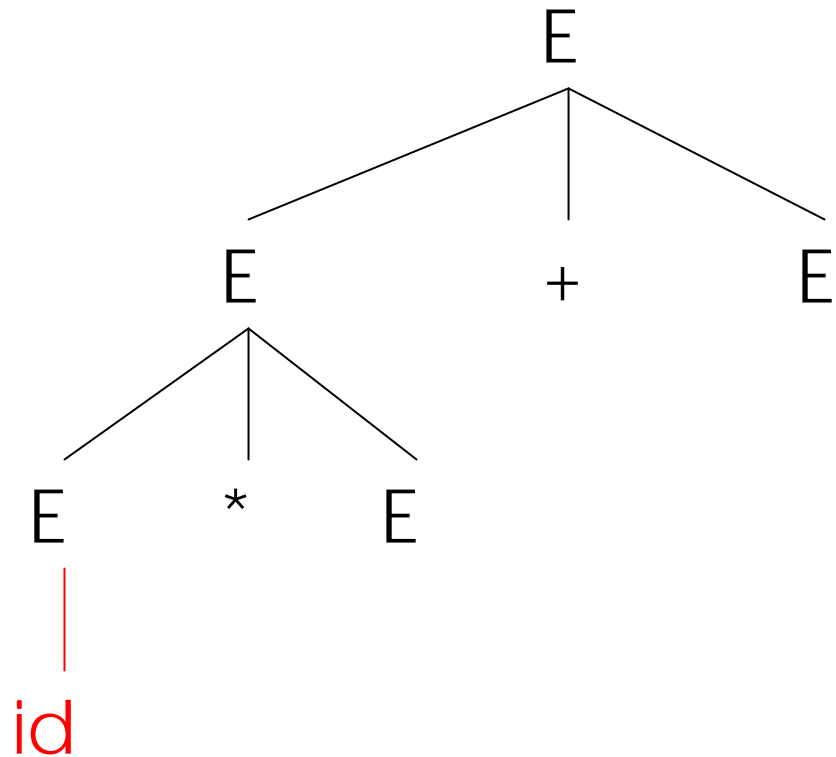
E
 $\rightarrow E+E$
 $\rightarrow E * E+E$



Derivation in Detail (4)

$E \rightarrow E+E \mid E * E \mid (E) \mid id$

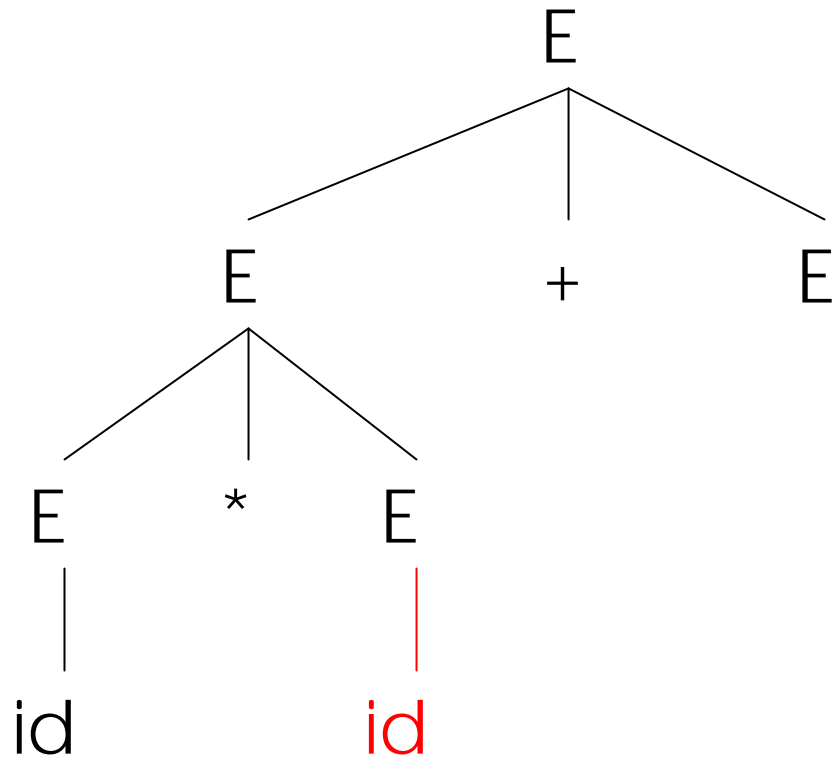
E
 $\rightarrow E+E$
 $\rightarrow E * E+E$
 $\rightarrow id * E + E$



Derivation in Detail (5)

$E \rightarrow E+E \mid E * E \mid (E) \mid id$

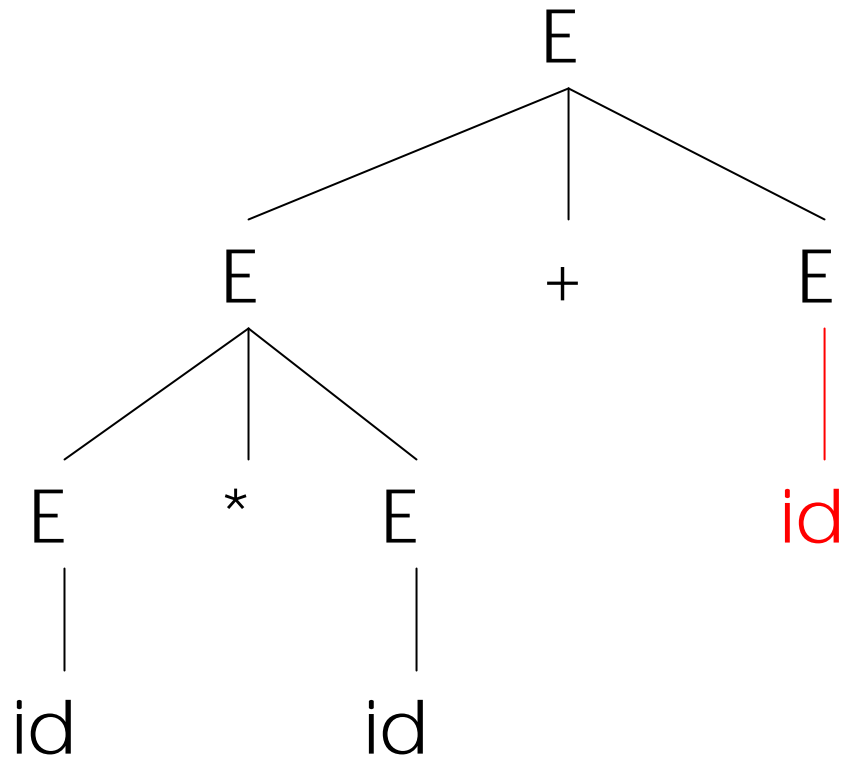
E
 $\rightarrow E+E$
 $\rightarrow E * E+E$
 $\rightarrow id * E + E$
 $\rightarrow id * id + E$



Derivation in Detail (6)

$E \rightarrow E+E \mid E * E \mid (E) \mid id$

E
 $\rightarrow E+E$
 $\rightarrow E * E+E$
 $\rightarrow id * E + E$
 $\rightarrow id * id + E$
 $\rightarrow id * id + id$



Notes on Derivations

- A parse tree has
 - Terminals at the leaves
 - Non-terminals at the interior nodes
- An in-order traversal of the leaves is the original input
- The parse tree shows the association of operations; the input string does not !

Left-most and Right-most Derivations

- What was shown before was a *left-most derivation*
 - At each step, we replaced the left-most non-terminal
- There is an equivalent notion of a *right-most derivation*
 - Shown on the right

$E \rightarrow E+E \mid E * E \mid (E) \mid id$

E
 $\rightarrow E+E$
 $\rightarrow E+id$
 $\rightarrow E * E + id$
 $\rightarrow E * id + id$
 $\rightarrow id * id + id$

Right-most Derivation in Detail (1)

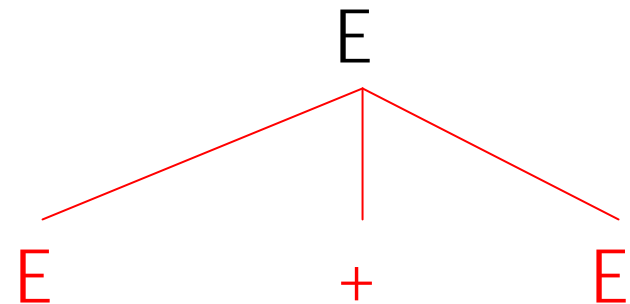
$E \rightarrow E+E \mid E^*E \mid (E) \mid \text{id}$

E

E

Right-most Derivation in Detail (2)

$E \rightarrow E+E \mid E * E \mid (E) \mid \text{id}$

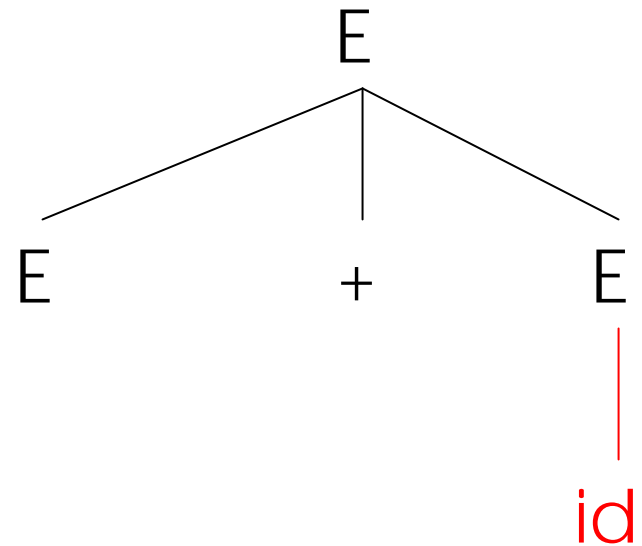


E
 $\rightarrow E+E$

Right-most Derivation in Detail (3)

$E \rightarrow E+E \mid E * E \mid (E) \mid id$

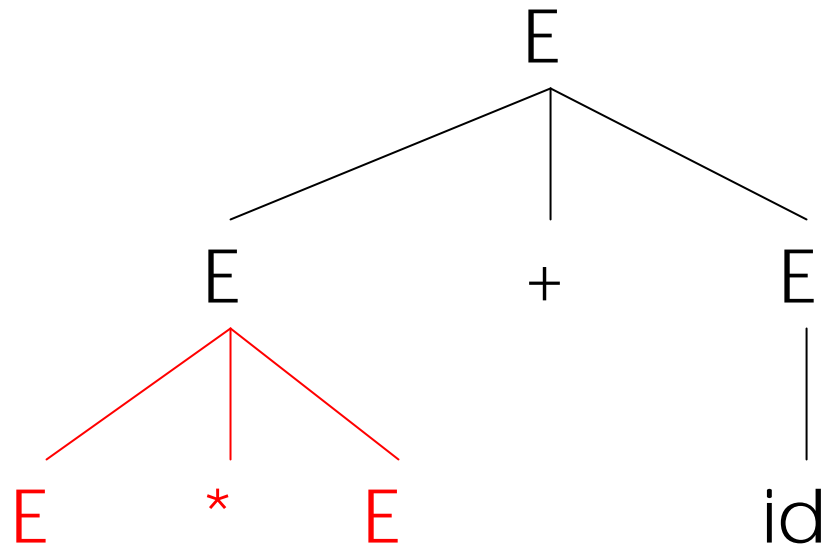
E
 $\rightarrow E+E$
 $\rightarrow E+id$



Right-most Derivation in Detail (4)

$E \rightarrow E+E \mid E * E \mid (E) \mid id$

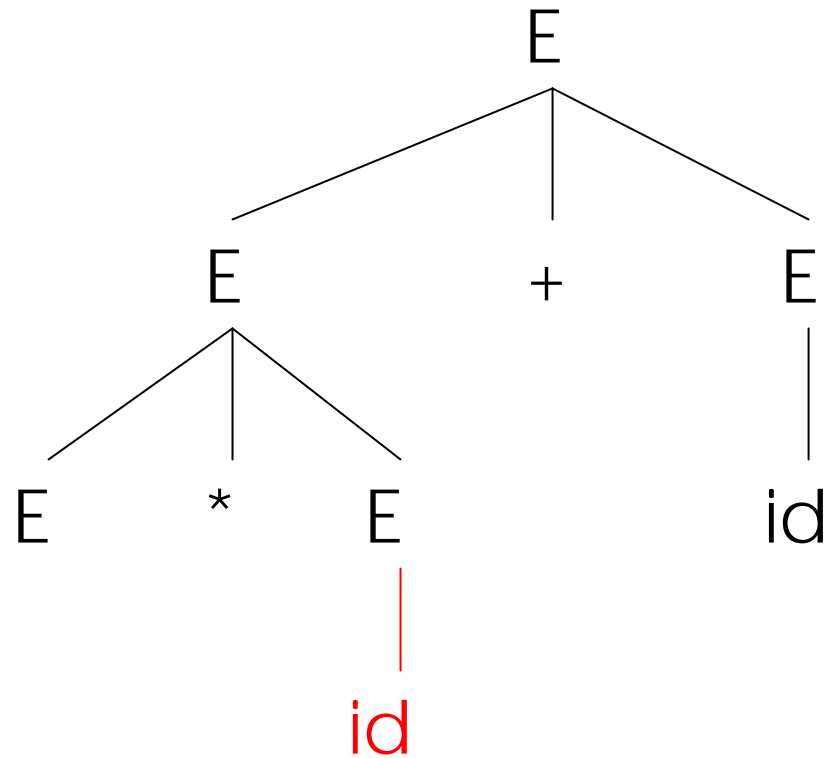
E
 $\rightarrow E+E$
 $\rightarrow E+id$
 $\rightarrow E * E + id$



Right-most Derivation in Detail (5)

$E \rightarrow E+E \mid E * E \mid (E) \mid id$

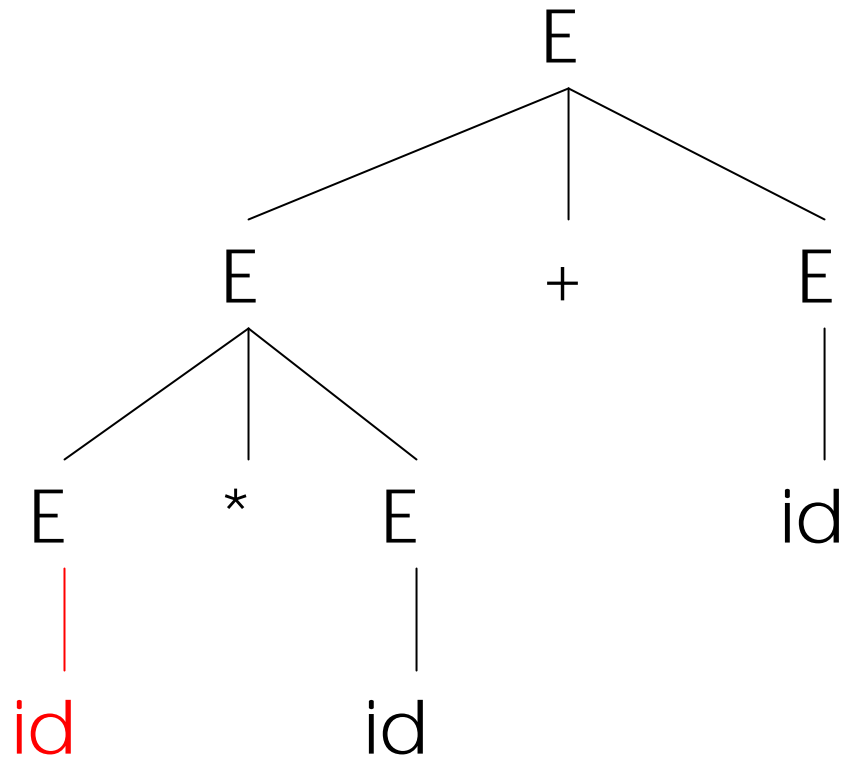
E
 $\rightarrow E+E$
 $\rightarrow E+id$
 $\rightarrow E * E + id$
 $\rightarrow E * id + id$



Right-most Derivation in Detail (6)

$E \rightarrow E+E \mid E * E \mid (E) \mid id$

E
 $\rightarrow E+E$
 $\rightarrow E+id$
 $\rightarrow E * E + id$
 $\rightarrow E * id + id$
 $\rightarrow id * id + id$



Derivations and Parse Trees

- Note that:
 - right-most and left-most derivations have the same parse tree
 - for each parse tree, there is a right-most and a left-most derivation
- The difference *is just in the order* in which branches are added

Summary of Derivations

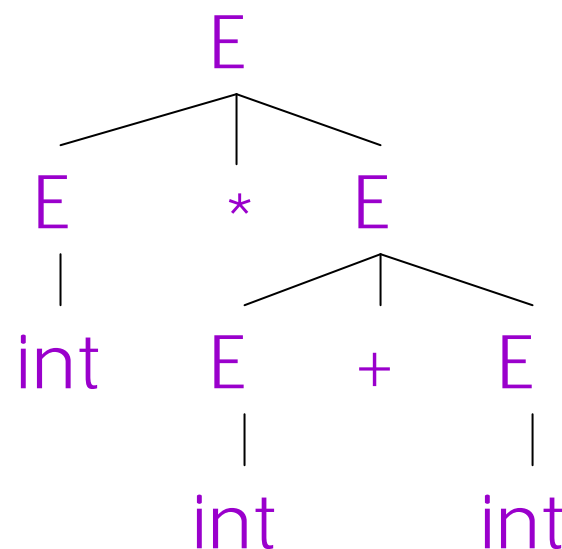
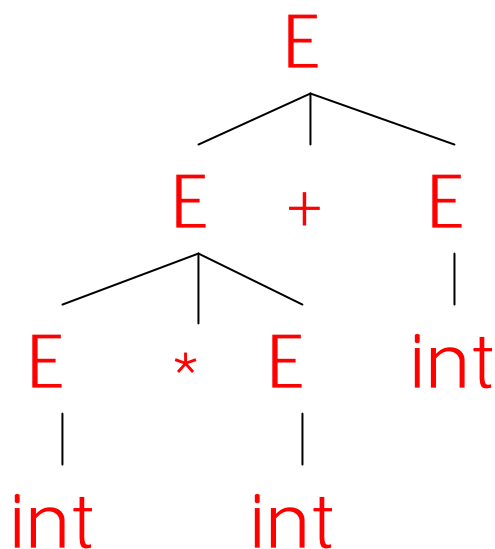
- We are not just interested in whether $s \in L(G)$
 - We need a parse tree for s
- A derivation defines a parse tree
 - But one parse tree may have many derivations
- Left-most and right-most derivations are important in parser implementation

Ambiguity

- Grammar:

$$E \rightarrow E + E \mid E * E \mid (E) \mid \text{int}$$

- The string $\text{int} * \text{int} + \text{int}$ has two parse trees



Ambiguity (Cont.)

- A grammar is *ambiguous* if it has more than one parse tree for some string
 - Equivalently, if there is more than one right-most or left-most derivation for some string
- Ambiguity is bad in programming languages
 - Leaves meaning of some programs ill-defined
- Ambiguity is common in programming languages
 - Arithmetic expressions
 - IF-THEN-ELSE

Dealing with Ambiguity

- There are several ways to handle ambiguity
- Most direct method is to rewrite the grammar unambiguously

$$E \rightarrow T + E \mid T$$

$$T \rightarrow \text{int} * T \mid \text{int} \mid (E)$$

- This grammar enforces precedence of * over +

Ambiguity: The Dangling Else

- Consider the following grammar

$$\begin{array}{l} S \rightarrow \text{if } C \text{ then } S \\ \quad | \text{if } C \text{ then } S \text{ else } S \\ \quad | \text{OTHER} \end{array}$$

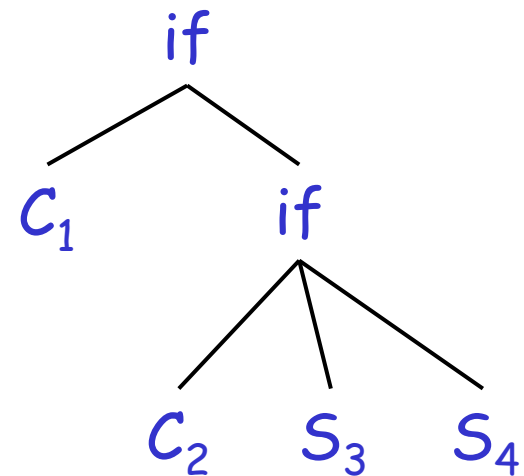
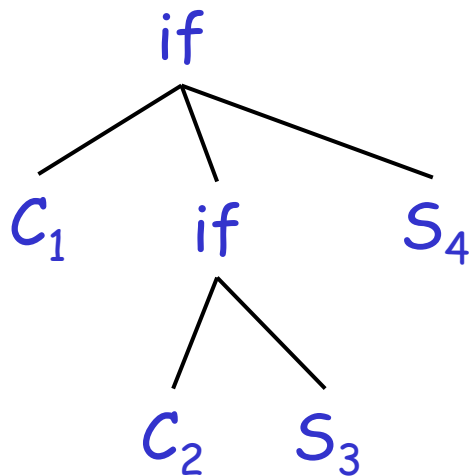
- This grammar is also ambiguous

The Dangling Else: Example

- The expression

if C_1 then if C_2 then S_3 else S_4

has two parse trees



- Typically we want the second form

The Dangling Else: A Fix

- `else` should match the closest unmatched `then`
- We can describe this in the grammar

$S \rightarrow$ MIF /* all `then` are matched */
 | UIF /* some `then` are unmatched */

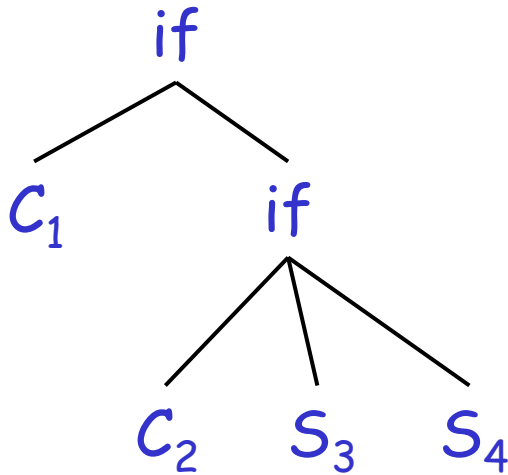
MIF \rightarrow if C then MIF else MIF
 | OTHER

UIF \rightarrow if C then S
 | if C then MIF else UIF

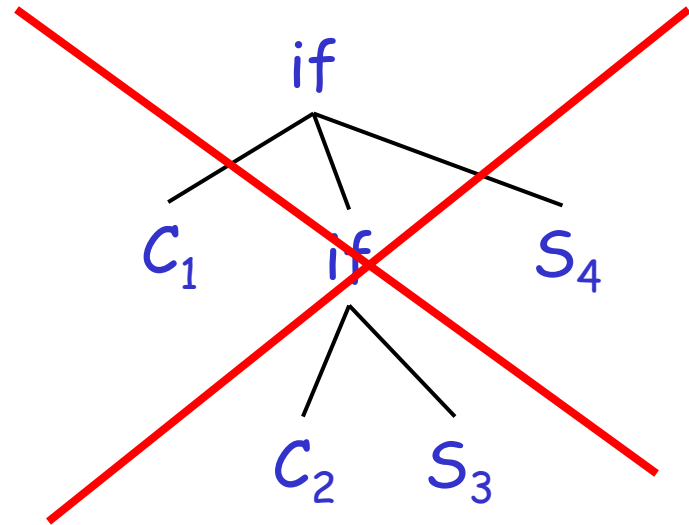
- Describes the same set of strings

The Dangling Else: Example Revisited

- The expression `if C1 then if C2 then S3 else S4`



- A valid parse tree (for a **UIF**)



- Not valid because the **then** expression is not a **MIF**

Ambiguity

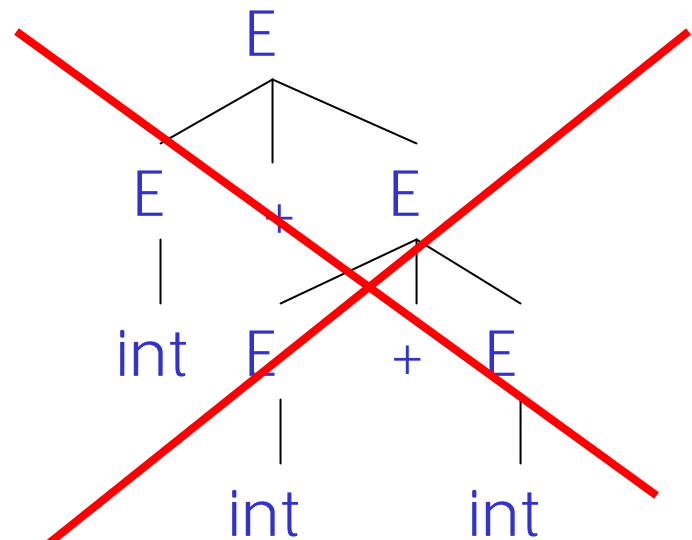
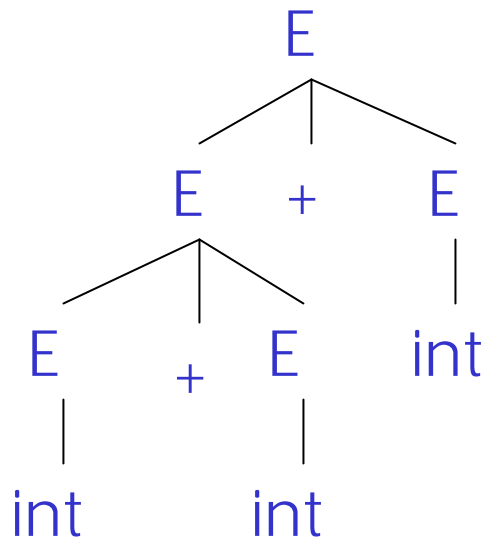
- No general techniques for handling ambiguity
- Impossible to convert automatically an ambiguous grammar to an unambiguous one
- Used with care, ambiguity can simplify the grammar
 - Sometimes allows more natural definitions
 - However, we need disambiguation mechanisms

Precedence and Associativity Declarations

- Instead of rewriting the grammar
 - Use the more natural (ambiguous) grammar
 - Along with disambiguating declarations
- Most tools allow precedence and associativity declarations to disambiguate grammars
- Examples ...

Associativity Declarations

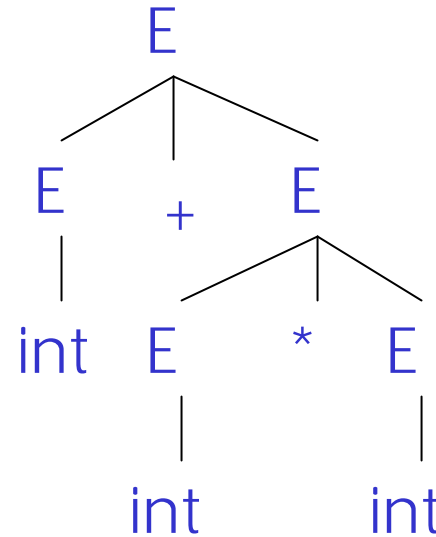
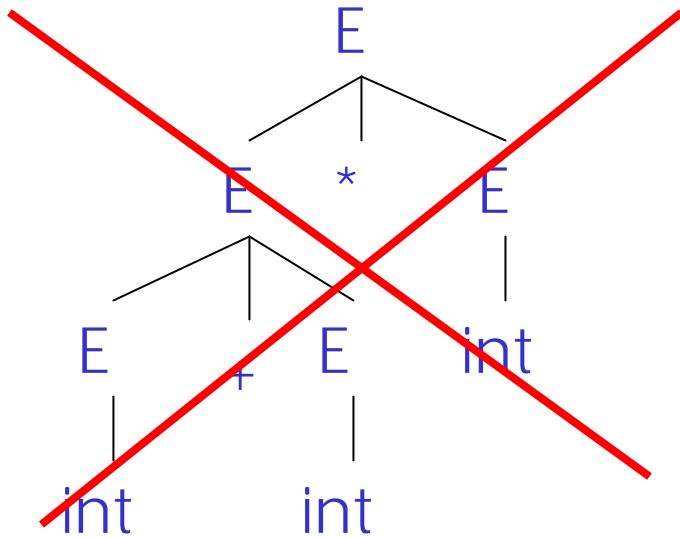
- Consider the grammar $E \rightarrow E + E \mid \text{int}$
- Ambiguous: two parse trees of $\text{int} + \text{int} + \text{int}$



- Left associativity declaration: `%left +`

Precedence Declarations

- Consider the grammar $E \rightarrow E + E \mid E * E \mid \text{int}$
And the string $\text{int} + \text{int} * \text{int}$



- Precedence declarations: `%left +`
`%left *`

Error Handling

- Purpose of the compiler is
 - To detect non-valid programs
 - To translate the valid ones
- Many kinds of possible errors (e.g. in C)

<u>Error kind</u>	<u>Example</u>	<u>Detected by ...</u>
Lexical	... \$...	Lexer
Syntax	... x *% ...	Parser
Semantic	... int x; y = x(3); ...	Type checker
Correctness	your favorite program	Tester/User

Syntax Error Handling

- Error handler should
 - Report errors accurately and clearly
 - Recover from an error quickly
 - Not slow down compilation of valid code
- Good error handling is not easy to achieve

Approaches to Syntax Error Recovery

- From simple to complex
 - Panic mode
 - Error productions
 - Automatic local or global correction

- Not all are supported by all parser generators

Error Recovery: Panic Mode

- Simplest, most popular method
- When an error is detected:
 - Discard tokens until one with a clear role is found
 - Continue from there
- Such tokens are called synchronizing tokens
 - Typically the statement or expression terminators

Syntax Error Recovery: Panic Mode (Cont.)

- Consider the erroneous expression

$(1 + + 2) + 3$

- Panic-mode recovery:
 - Skip ahead to next integer and then continue
- (ML)-Yacc: use the special terminal **error** to describe how much input to skip

$E \rightarrow \text{int} \mid E + E \mid (E) \mid \text{error int} \mid (\text{error})$

Syntax Error Recovery: Error Productions

- Idea: specify some recovery rules in the grammar based on known common mistakes
- Essentially promotes common errors to alternative syntax
- Example:
 - Write $5x$ instead of $5 * x$
 - Add the production $E \rightarrow \dots \mid EE$
- Disadvantage
 - Complicates the grammar

Syntax Error Recovery: Past and Present

- (Distant) Past
 - Slow recompilation cycle (even once a day)
 - Find as many errors in one cycle as possible
 - Researchers could not let go of the topic
- Present
 - Quick recompilation cycle
 - Users tend to correct one error/cycle
 - Complex error recovery is needed less
 - Panic-mode seems enough